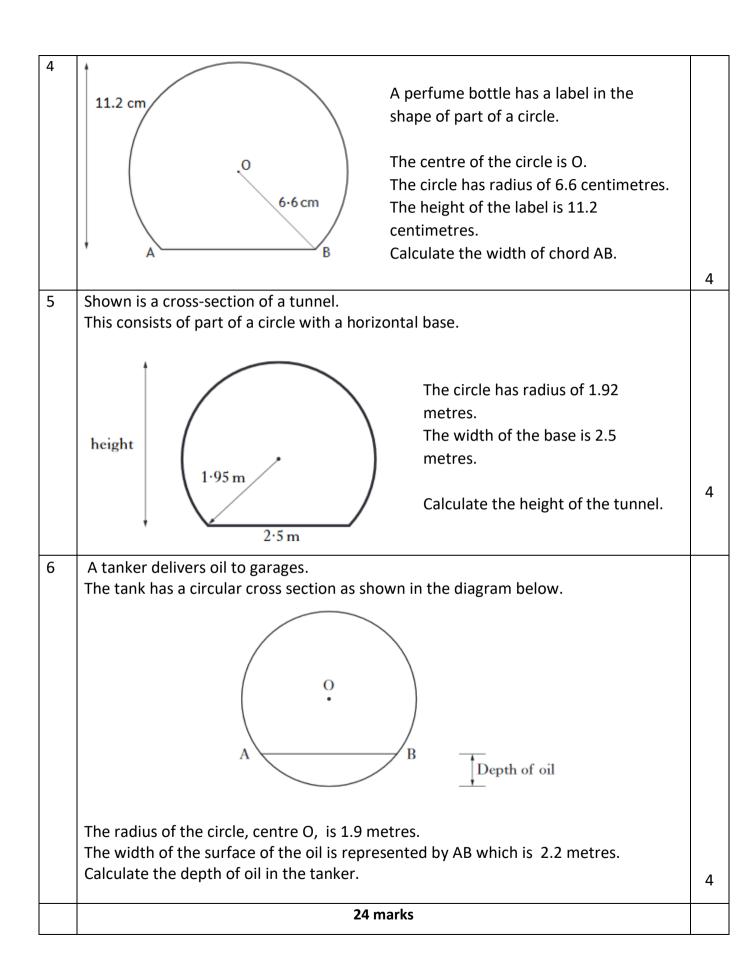
	Pythagoras in the circle	
1	The shape shown is part of a circle with a centre O.	
	The circle has radius of 13 centimetres. AB is a chord of length 20 centimetres.	
	Calculate the width of the shape.	4
2	The diagram shows the circular cross-section of a milk tank.	
	 Depth of milk The radius of the circle, centre O, is 1.6 metres The depth of milk in the tank is 2.7 metres. 	
	Calculate the width of the surface of the milk, represented by chord ML.	4
3	The diagram shows a cross-section of a tunnel. This consists of part of a circle with a centre O and a horizontal base. The circle has radius of 1.7 metres. Chord XY is 1.8 metres. Calculate the height of the tunnel.	4



	Pythagoras in the circle – Answers	
1	Mark 1 Recognise right angled triangle	
	13 10 x	
	Mark 2 consistent statement of Pythagoras $x^2 = 13^2 - 10^2$ Mark 3 calculate a value for the missing side $x = 8.3$ Mark 4 calculate the width $x = 8.3$	
	2 marks can be given for $x^2=13^2+10^2, x=16.4$ so width is $29.4~cm$ 2 marks can be given for $x^2=20^2-13^2, x=15.2$ so width is $28.2~cm$	4
2	Mark 1 Recognise right angled triangle	
	1.1 1.6	
	Mark 2 consistent statement of Pythagoras $x^2 = 1.6^2 - 1.1^2$ Mark 3 calculate a value for the missing side $x = 1.16$ Mark 4 Calculate the width $2 \times 1.16 = 2.32 m$	
	2 marks can be given for $x^2 = 1.6^2 + 1.1^2$, $x = 1.94$, so width is $2 \times 1.94 = 3.88 m$ 2 marks can be given for $x^2 = 2.7^2 - 1.6^2$, $x = 2.17$, so width is $2 \times 2.17 = 4.34 m$	4
3	Mark 1 Recognise right angled triangle 1.7 x 0.9	
	Mark 2 consistent statement of Pythagoras $x^2 = 1.7^2 - 0.9^2$ Mark 3 calculate a value for the missing side $x = 1.44$ Mark 4 Calculate the height $x = 1.44 = 3.14 m$	
	2 marks can be given for $x^2 = 1.7^2 + 0.9^2$, $x = 1.9$, so height is $1.7 + 1.9 = 3.6 m$ 2 marks can be given for $x^2 = 1.8^2 - 1.7^2$, $x = 0.6$, so height is $1.7 + 0.6 = 2.3 m$	4

4	Mark 1 Recognise right angled triangle 6.6 x	
	Mark 2 consistent statement of Pythagoras $x^2 = 6.6^2 - 4.6^2$	
	Mark 3 calculate a value for the missing side $x = 4.7$	
	Mark 4 Calculate the width $2 \times 4.7 = 9.4 \ cm$	
	2 marks can be given for $x^2 = 6.6^2 + 4.6^2$, $x = 8$, so width is $2 \times 8 = 16$ cm 2 marks can be given for $x^2 = 11.2^2 - 6.6^2$, $x = 9$, so width is $2 \times 9 = 18$ cm	4
5	Mark 1 Recognise right angled triangle	
	1.95 x	
	1.25	
	Mark 2 consistent statement of Pythagoras $x^2 = 1.95^2 - 1.25^2$	
	Mark 3 calculate a value for the missing side $x = 1.5$ Mark 4 Calculate the height $1.95 + 1.5 = 3.45 m$	
	Walk 4 Calculate the neight	
	2 marks can be given for $x^2 = 1.95^2 + 1.25^2$, $x = 2.3$, so height is $1.95 + 2.3 = 4.25$ m 2 marks can be given for $x^2 = 2.5^2 - 1.95^2$, $x = 1.6$, so height is $1.95 + 1.6 = 3.55$ m	4
6	Mark 1 Recognise right angled triangle	
	1.9 m x 1.1m	
	Mark 2 consistent statement of Pythagoras $x^2 = 1.9^2 - 1.1^2$	
	Mark 3 calculate a value for the missing side $x = 1.5$ Mark 4 Calculate the depth $1.9 - 1.5 = 0.4 \ \mathbf{m}$	
	·	
	2 marks can be given for $x^2 = 1.9^2 + 1.1^2$, $x = 16.4$ so depth is $1.9 - 2.2 = -0.3 m$	
	2 marks can be given for $x^2 = 2.2^2 - 1.9^2$, $x = 1.1$ so depth is $1.9 - 1.1 = 0.8$ m	4
L	1	

SI S4 Nat 5 2021